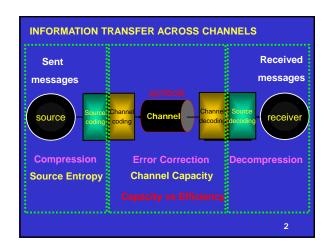
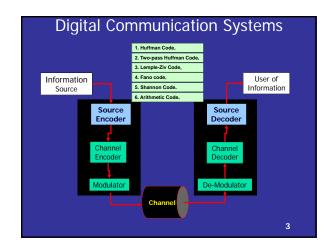


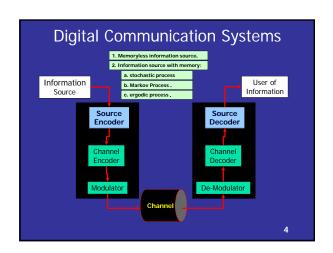
Today's Topics

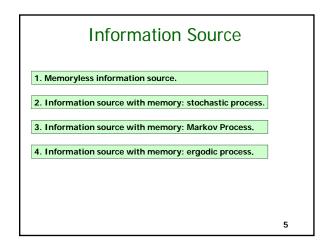
- · Memoryless information source.
- · Information source with memory:
 - stochastic process
 - Markov Process
 - ergodic process

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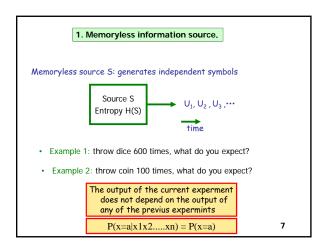




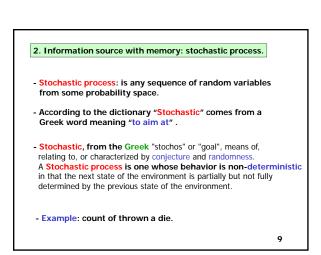


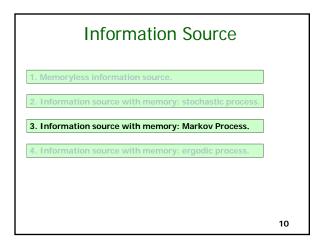


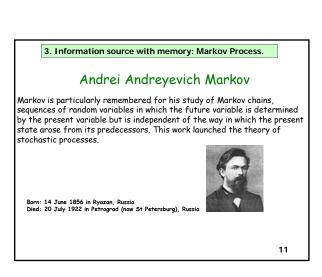
Information Source 1. Memoryless information source. 2. Information source with memory: stochastic process. 3. Information source with memory: Markov Process. 4. Information source with memory: ergodic process.

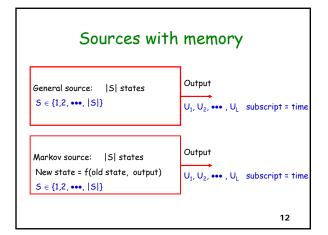


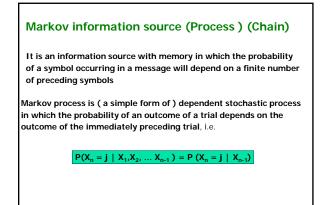
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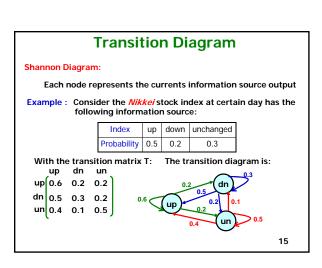
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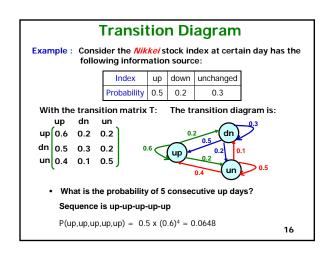
Markov information source (Process) (Chain)

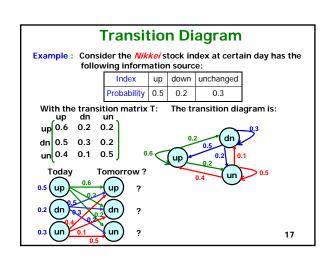
Let an experiment has a finite number of n possible outcomes $A = \{ a_1, ..., a_n \} \text{ called } states.$ For a Markov process we specify a table of probabilistic associated with transitions from any state to another.

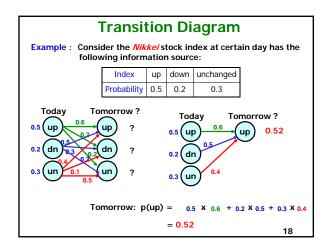
This is called probability transition matrix T.

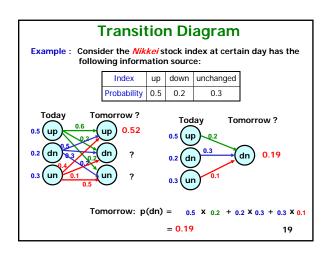
For a Markov information source S = (A, T), T has the form: $a_1 \qquad a_2 \qquad \dots \qquad a_n$ $a_1 \qquad p(a_1|a_1) \quad p(a_2|a_1) \quad \dots \qquad p(a_n|a_1) \quad p(a_n|a_2) \quad \dots \quad p(a_n|a_2) \quad \dots \quad p(a_n|a_n)$ $T = \begin{pmatrix} a_1 & a_2 & \dots & a_n \\ p(a_1|a_2) & p(a_2|a_2) & \dots & p(a_n|a_2) \\ p(a_1|a_n) & p(a_2|a_n) & \dots & p(a_n|a_n) \end{pmatrix}$

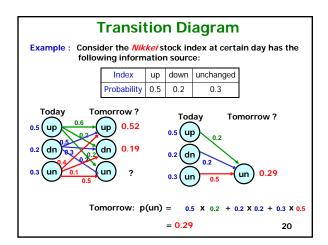


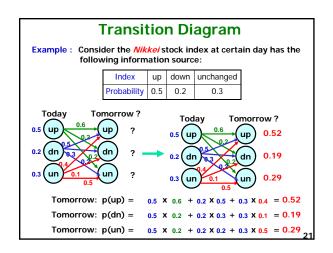


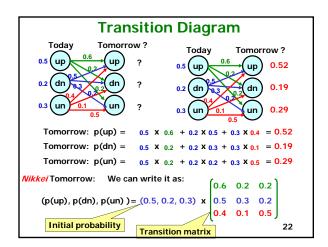


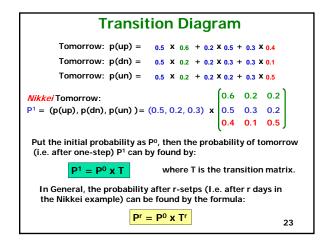


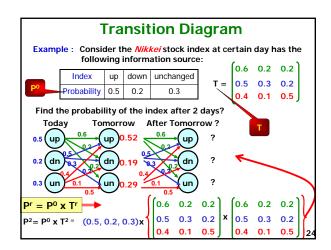


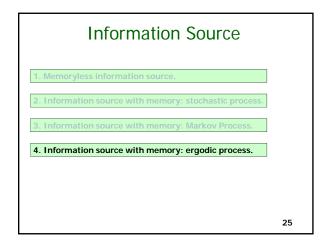












Ergodic Markov Process A Markov chain is said to be *ergodic* if, after a certain finite number of steps, it is possible to go from any state to any other state with a nonzero probability. The following figure shows the relationship between processes: Stochastic Markov Ergodic

Ergodic Markov Process To check that some Markov process is ergodic: 1. We check the transition diagram for this process 2. if, from any state, we can reach all other states, then the process is ergodic 3. if some state(s) are not reachable from any other state, then the process is NOT ergodic

