Automata and formal languages Exercise

Answer the following questions and submit your report by next week.

1. Let $\Sigma = \{a, b\}$, define $n_a, n_b : \Sigma^* \to N$ (where N is the set of natural numbers) such that $n_a(w)$ is the number of a's in w and $n_b(w)$ is the number of b's in w. Show that the following languages are not regular

(a)
$$L_1 = \{w : n_a(w) = n_b(w)\}$$

(b)
$$L_2 = \{ w : n_a(w) \neq n_b(w) \}$$

- 2. Show that the language $\{0^n 10^n : n \ge 1\}$ is not a regular language.
- 3. Construct a finite automaton that accepts the language generated by the grammar:

$$\begin{array}{rccc} S & \longrightarrow & aaS | aA \\ A & \longrightarrow & abS | b \end{array}$$

4. Construct a right-linear grammar that accept the language:

 $L=\{w: w \text{ has both an even number of } 0's \text{ and} an even number of } 1's\}$